



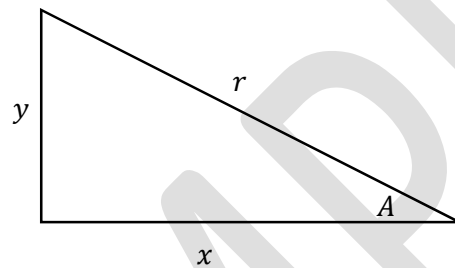
# AdeTom Tutors

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Grade 12 Mathematics

## Practice Exercise – Trigonometry

1. Given the following sketch, prove that  $\tan A = \frac{\sin A}{\cos A}$



2. Simplify the following

- $\sin^2 200^\circ + \cos^2 200^\circ$
- $\frac{\sin^2 B}{(1 + \cos B)}$
- $\frac{1 - \sin^2 T}{1 - \sin T}$
- $\cos(180^\circ - A)$
- $\sin(180^\circ - A)$
- $\sin(720^\circ - A)$
- $\tan(360^\circ - A)$
- $\cos(A + 540^\circ)$
- $\sin(-A)$
- $\cos(-135^\circ)$
- $\sin(-150^\circ)$
- $\sin(A + 720^\circ)$
- $\cos(x - 360^\circ)$
- $\sin(x - 180^\circ)$
- $\tan(x - 360^\circ)$
- $\cos(-x - 720^\circ)$
- $\sin(90^\circ - x)$
- $\cos(90^\circ + x)$

- s)  $\sin(630^\circ - x)$
- t)  $\cos(z - 90^\circ)$
- u)  $\tan(z - 90^\circ)$
- v)  $\sin(z - 450^\circ)$
- w)  $\cos(450^\circ + z)$
- x)  $\sin(z + 180^\circ)$

3. Expand the following

- a)  $\cos(x - 50^\circ)$
- b)  $\sin(62^\circ)$  if  $\sin 2^\circ = k$
- c)  $\cos 25^\circ$  if  $\cos 5^\circ = p$
- d)  $\sin(30 + 40^\circ)$

4. Use  $\cos 2A = \cos^2 A - \sin^2 A$ , to proof the following

- a)  $\cos 2A = 2\cos^2 A - 1$
- b)  $\cos 2A = 1 - 2\sin^2 A$

5. Simplify the following

- a)  $\frac{\sin 70^\circ}{\cos 20^\circ}$
- b)  $\frac{\sin 40^\circ}{\cos 50^\circ}$
- c)  $\frac{\sin 10^\circ}{\cos 80^\circ}$
- d)  $\sin^2(180^\circ - P)$
- e)  $\cos^2(360^\circ - P)$
- f)  $\tan(90^\circ - P)$
- g)  $\tan 2P$
- h)  $\sin 930^\circ$
- i)  $\tan 870^\circ$
- j)  $\cos 1485^\circ$
- k)  $\sin(1440^\circ - P)$
- l)  $\cos(180^\circ)$
- m)  $\sin(360^\circ)$
- n)  $\tan(270^\circ)$
- o)  $\cos(-180^\circ)$
- p)  $\cos 75^\circ$
- q)  $\sin 15^\circ$
- r)  $\cos 105^\circ$
- s)  $\cos 35^\circ \cos 20^\circ - \sin 35^\circ \sin 20^\circ$
- t)  $\cos(x - 300^\circ) - \sin(x - 150^\circ)$

6. Given  $17\sin x - 8 = 0$ , where  $90^\circ \leq x \leq 270^\circ$ . Determine

- a)  $\sin 2x$
- b)  $\cos 2x$
- c)  $\tan 2x$

- d)  $\cos(90^\circ - x)$
- e)  $\sin(x - 45^\circ)$
- f)  $\cos(x + 60^\circ)$
- g)  $\tan(90^\circ + x)$

7. Given that  $\cos 26^\circ = k$ , determine the following in terms of  $k$

- a)  $\tan 56^\circ$
- b)  $\sin 26^\circ$
- c)  $\cos 254^\circ$
- d)  $\sin 386^\circ$
- e)  $\cos 207^\circ$
- f)  $\sin 64^\circ$
- g)  $\tan 64^\circ$
- h)  $\sin(-26)$
- i)  $2\cos^2 10^\circ - 1$

8. Given that  $\tan x = p$ , show that  $\sin 2x = \frac{2p}{p^2+1}$

9. Simplify the following

- a)  $\frac{\tan(180^\circ+A) \cos(180^\circ-A) \sin(360^\circ-A)}{\cos(90^\circ-A)}$
- b)  $\frac{\tan(180^\circ+A) \cos(360^\circ-A)}{\sin(180^\circ-A) \cos(90^\circ+A) + \cos(540^\circ+A) \cos(-A)}$
- c)  $\cos(90^\circ - 2A) \tan(180^\circ + A) \sin^2(A - 360^\circ)$
- d)  $\frac{\sin(90^\circ+Q) + \cos 180^\circ \sin(-Q)}{\sin(180^\circ) - \tan 135^\circ}$
- e)  $(\sqrt{2}\cos 75^\circ - 1)(1 + \sqrt{2}\cos 75^\circ)$
- f)  $\frac{\sin 33^\circ}{\sin 11^\circ} - \frac{\cos 33^\circ}{\cos 33^\circ}$

10. Prove the following identities

- a)  $\frac{1-2\sin B \cos B}{\sin B - \cos B} = \sin B - \cos B$
- b)  $\frac{1-\tan A}{1+\tan A} = \frac{\cos 2A}{1+\sin 2A}$
- c)  $\frac{\sin 2x}{\cos 2x + \sin^2 x} = 2 \tan x$
- d)  $\frac{\sin x}{1-\cos x} - \frac{\cos x}{\sin x} = \frac{1}{\sin x}$
- e)  $\frac{\sin 2x}{\sin x} - \frac{\cos 2x}{\cos x} = \frac{1}{\cos x}$
- f)  $\frac{1-\cos 2x - \sin x}{\sin 2x - \cos x} = \tan x$
- g)  $\frac{\sin(180^\circ+x) \tan(x-360^\circ) \cos 38^\circ}{\tan(360^\circ-x) \sin(x-180^\circ) \cos 240^\circ \tan 225^\circ \sin 488^\circ} = -2$
- h)  $\frac{\cos^2(90^\circ+\alpha)}{\cos(-\alpha) + \sin(90^\circ-\alpha) \cos \alpha} = \frac{1}{\cos \alpha} - 1$